

Optical Filters – Specifying Filters

MPI CBG Seminar

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Content

1. Filter specifications (bandpass, longpass, shortpass,...)
2. Transmitted and reflected wavefront errors
3. Angle of incidence and cone angles
4. Optical density
5. Dispersion
6. Polarization
7. Combining filters

:: Filter specifications

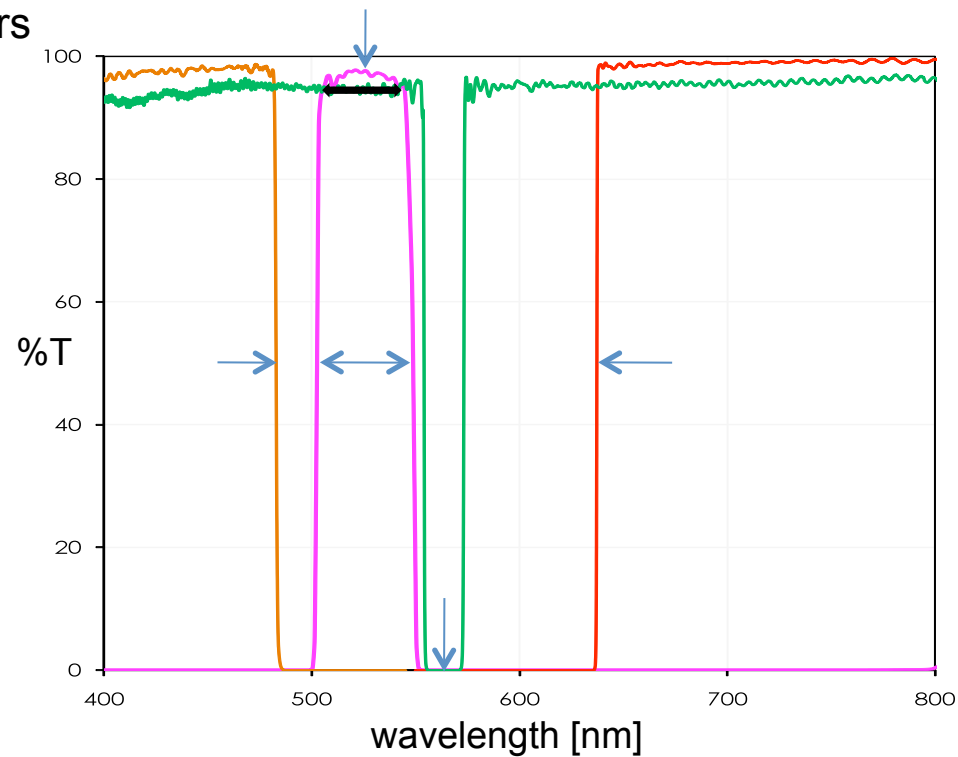
Filters and beamsplitters

:: Bandpass 525/50

:: Longpass 640 LP

:: Shortpass 490 SP

:: Notch 561 nm



Define:

:: CWL or notch wavelength

:: FWHM

:: GMBW*

:: Cut-on

:: Cut-off

:: Blocking range

:: AOI (angle of incidence)

*FWHM=GMBW+
0,01xCWL

:: Transmitted and reflected wavefront errors

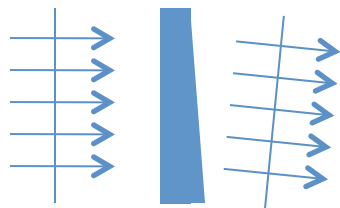
Wavefront distortion

:: $WD = TWD + RWD$ (transmitted and reflected wavefront distortion)

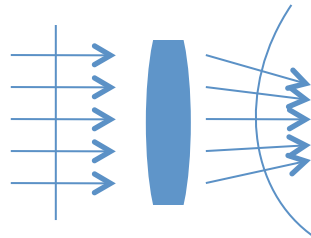
TWD caused by:

:: non plane-parallelity and / or lense effects due to thickness deviations

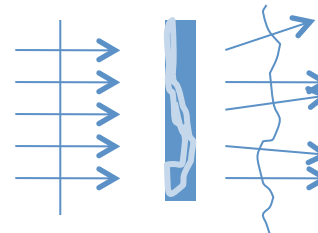
:: inhomogenities of the substrate (refraction index change)



wedge



lense



inhomogenities

:: Transmitted and reflected wavefront errors

Wavefront distortion

:: inhomogenities effect the image quality

:: lense effects cause focal shift and spot broadening

:: wedge effects cause pixel-shift

every optical component in the image pathway is responsible for the pixelhifft

$$pixelshif \approx 0,005 \frac{tubelength * \Sigma beamdeviation}{pixelspacing}$$

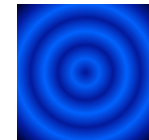
e.g. tubelength in a microscope ~ 200 mm, pixel spacing of the camera ~6,7 µm

=> less than 1 pixel shift for beam deviation < 7 arcsec

:: Transmitted and reflected wavefront errors

Transmitted wavefront distortion

- :: TWD is specified as absolute peak-to-peak error or RMS error, measured with a interferometer at 546 nm (ISO standard)
- :: RMS (root-mean-square) is used when irregularities dominate the flatness
RMS = $\frac{1}{4}$ absolute peak-to-peak error
- :: for filters $\frac{1}{4} \lambda$ 1λ RMS mostly fits
- :: for most filters the transmitted wavefront distortion matters, there is no need to specify any reflected wavefront distortion



:: Transmitted and reflected wavefront errors

Reflected wavefront distortion

:: Deviation of the perfect wavefront reflected off a surface relative to a perfectly plane surface

$$\text{RWD} = 2 \times \text{Flatness error}$$

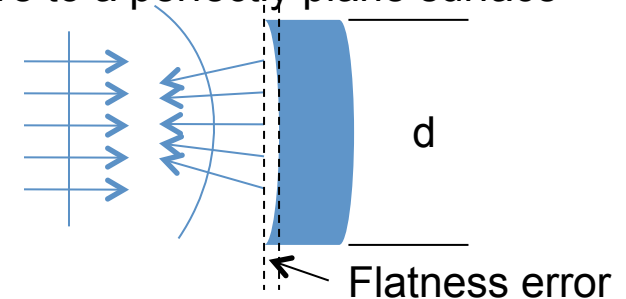
:: mostly caused by bent substrates

:: only matters when a filter or beamsplitter is used in a reflection geometry (microscope beamsplitter, image splitting)

:: bent filters act like lenses with a focal length of Radius/2

$$f = r/2 \Rightarrow f = d^2/\text{RWD} \quad (d = \text{diameter of the region where the flatness is specified})$$

:: e.g. beamsplitter $d = 20\text{mm} = 0,02\text{m}$; flatness error = $5\mu\text{m} = 0,000005\text{m} \Rightarrow f = 40\text{m}$

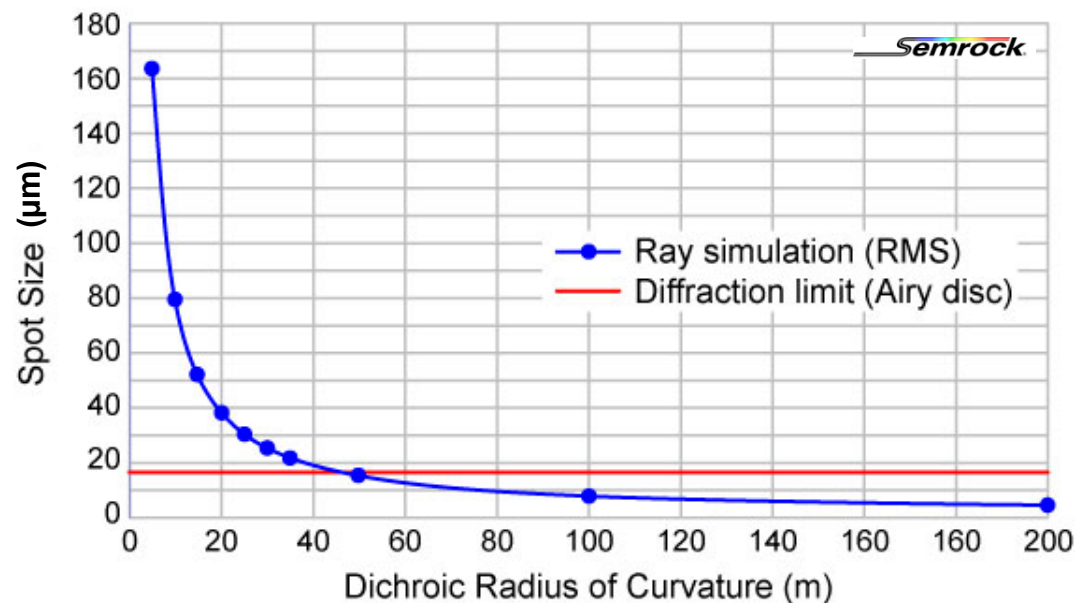


:: Transmitted and reflected wavefront errors

Reflected wavefront distortion

:: focal shift due to bent optics causes
an increase of the spot size
e.g. 40x objective, NA 0,75
focal length of tube lens = 200 mm
wavelength 510 nm

:: for most beamsplitters $\frac{1}{4} \lambda$ RMS
is sufficient (TIRF, image splitting,...)



:: Angle of incidence and cone angles

Influence of AOI and CHA

:: interference filters are mostly used under an angle of incidence AOI = 0 degree

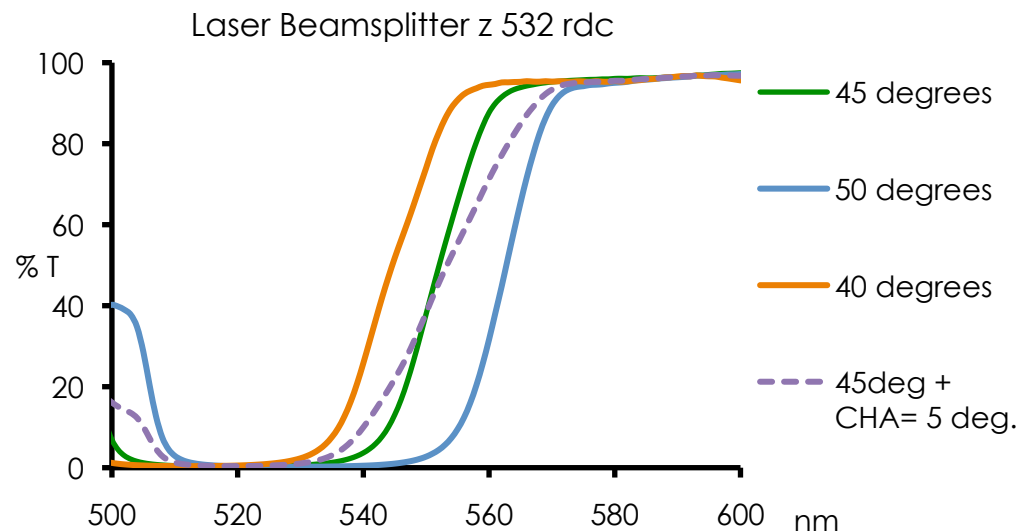
AOI > 0° causes shift according to:

$$\lambda(\text{AOI}) = \lambda_0 \sqrt{1 - (\sin(\text{AOI})/n_{\text{eff}})^2}$$

:: cone angles or cone half angles (CHA)

$$\lambda_{(\text{CHA})} = \sum_{\text{AOI}} \lambda(\text{AOI})$$

n_{eff} = effective refractive index
(polarization matters)



:: Optical density

Optical density OD

:: $OD = -\log(\text{Transmission})$

Blocking range of a fluorescence filter depending on

:: the light source => exciter

blocking must cover the emission range of the lightsource out of transmission band

:: detector => emitter

must suppress the transmitted light of the exciter

:: exciter and emitter must block each other with min. OD 6

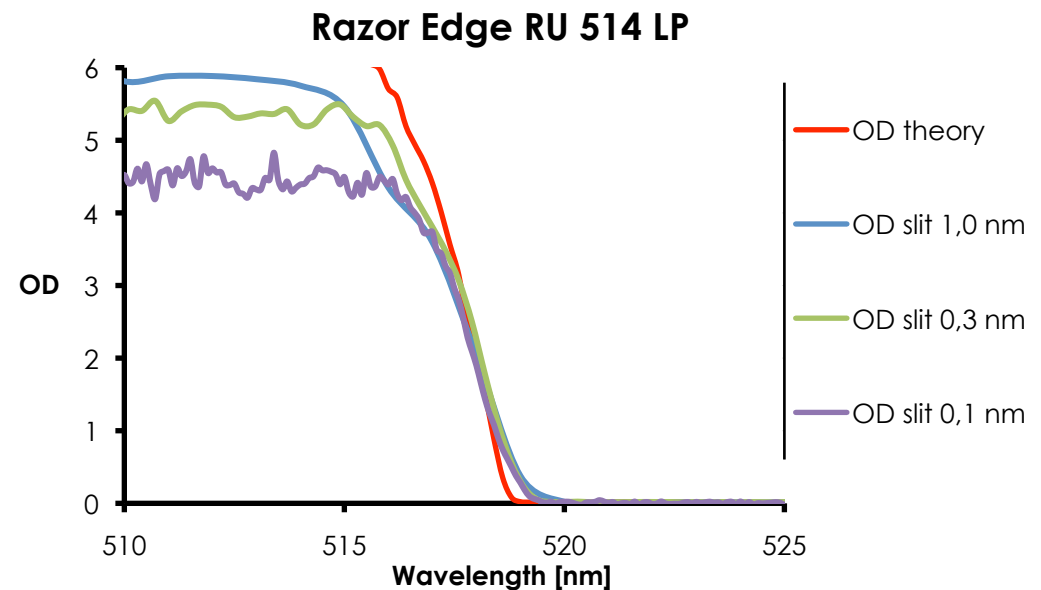
:: Optical density

Measuring optical density

:: spectrometer with double monochromator and PMT

:: limitations:

- noise limit ~ OD 6
- rounding of steep edges by slit width
- side lobes of the measuring beam (depends on spectrometer design)
- reduced slit width causes noise



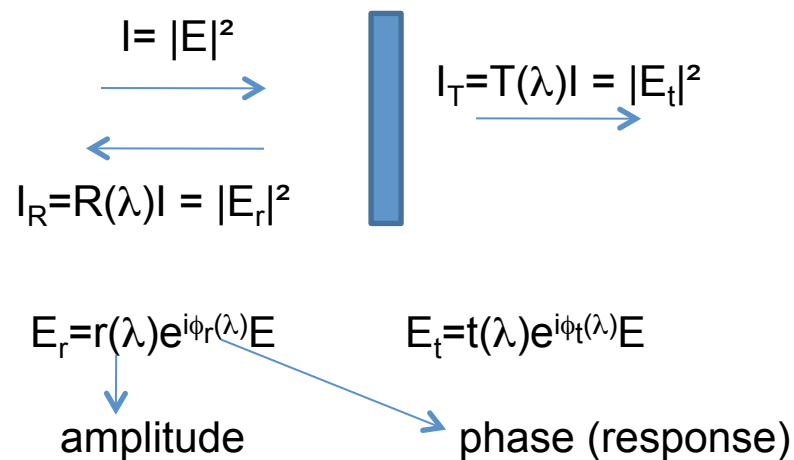
:: Dispersion

Consider dispersion when filters

:: are used in an interferometer

:: transmit or reflect a short pulse ($\ll 1$ ps)

=> are used in optical systems which are sensitive to the phase of the light



I intensity

E electrical field

$T(\lambda)$ and $R(\lambda)$ intensity transmission and reflection coefficients

$r(\lambda)e^{i\phi_r(\lambda)}$ amplitude reflection

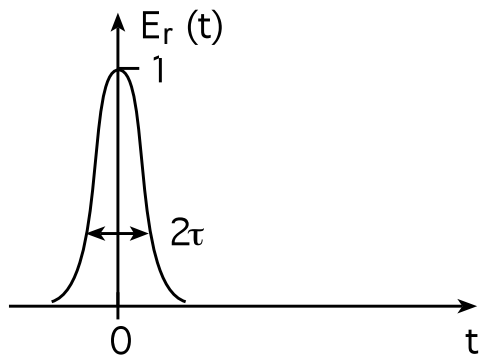
$t(\lambda)e^{i\phi_t(\lambda)}$ amplitude transmission

:: Dispersion

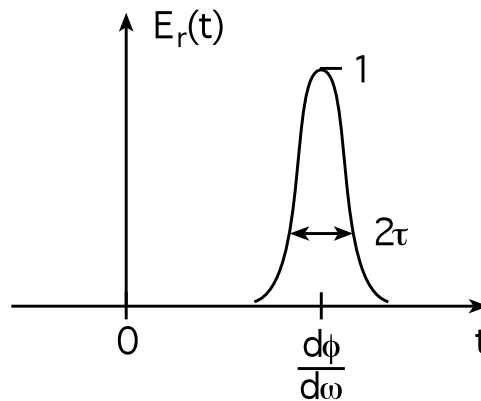
phase response $e^{i\phi_r(\lambda)}$ can be written as:

$$\phi_r(\omega) = \phi_r(\omega_0) + (\omega - \omega_0) \frac{\partial \phi_r}{\partial \omega} \bigg|_{\omega_0} + \frac{1}{2} (\omega - \omega_0)^2 \frac{\partial^2 \phi_r}{\partial \omega^2} \bigg|_{\omega_0} \quad \omega = \frac{2\pi c}{\lambda}$$

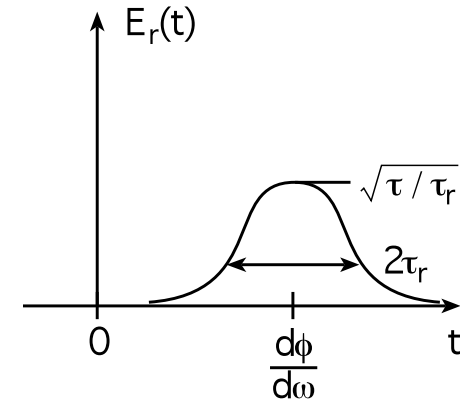
constant phase



time delay



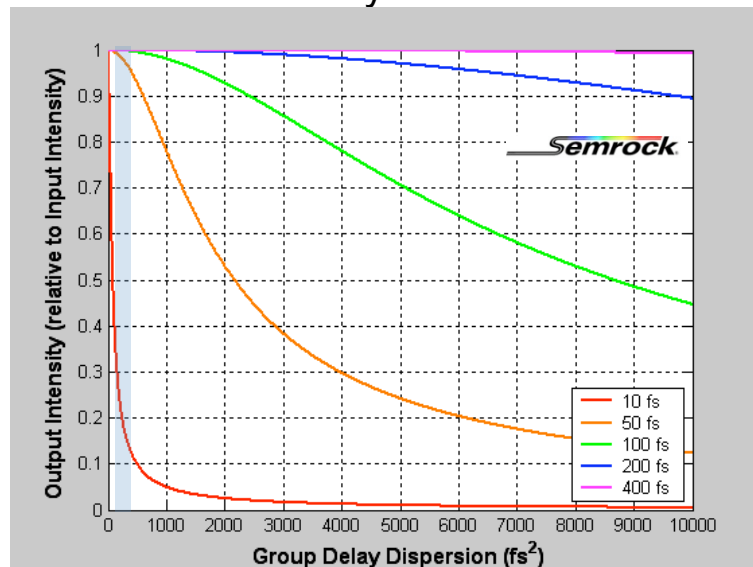
group delay dispersion
(pulse broadening)



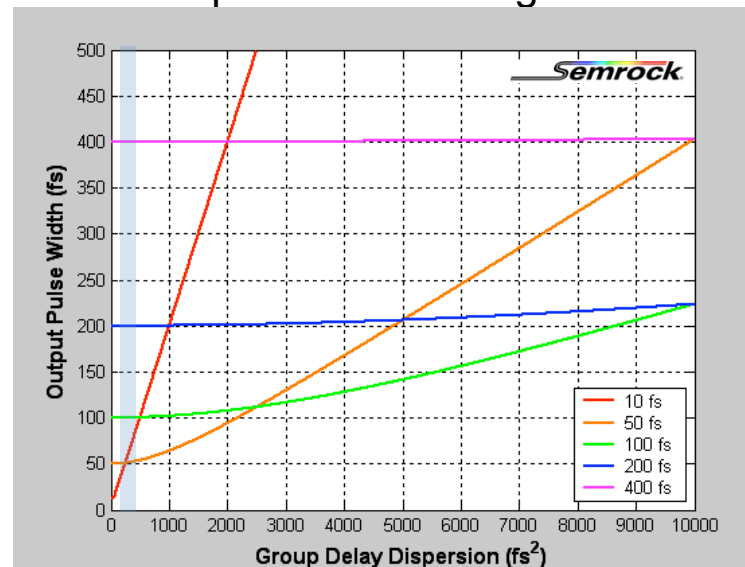
:: Dispersion

:: what happens in real life with e.g. multiphoton filters and beamsplitters?

intensity loss



pulse broadening



:: Polarization

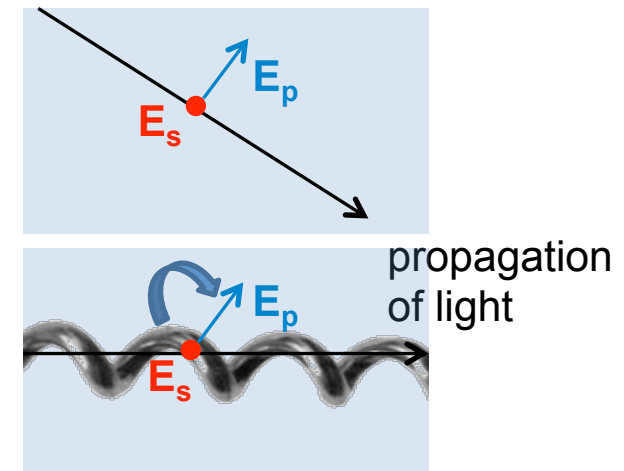
Polarization states:

:: linear polarization

s-polarization (E perpendicular to the plane of incidence)

p-polarization (E parallel to the plane of incidence)

:: circular polarization or more general elliptical polarization



:: Polarization

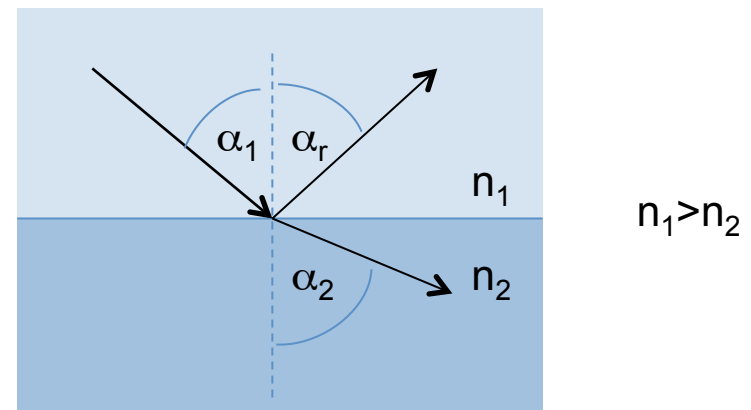
Some general optical laws

:: law of reflection $\alpha_1 = \alpha_r$

:: law of refraction $n_1 \sin \alpha_1 = n_2 \sin \alpha_2$ (Snell's law)

:: law of total reflection $\alpha_{critical} = \arcsin\left(\frac{n_2}{n_1}\right)$

:: Transmission = 1 - Reflection



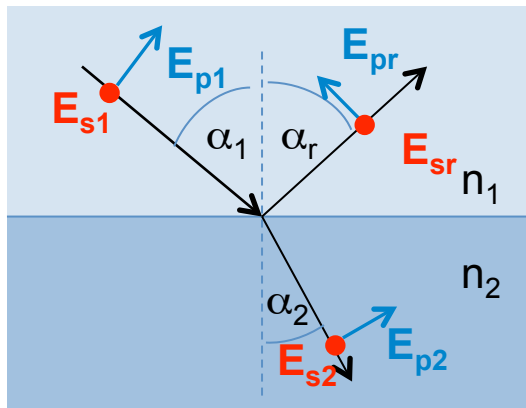
:: Polarization

Reflection for different polarization states

:: different polarizations are reflected by different amounts => Fresnel reflection

:: each polarization state has to be processed separately

:: amplitude reflection coefficient r and reflection R (reflectivity) is described by:

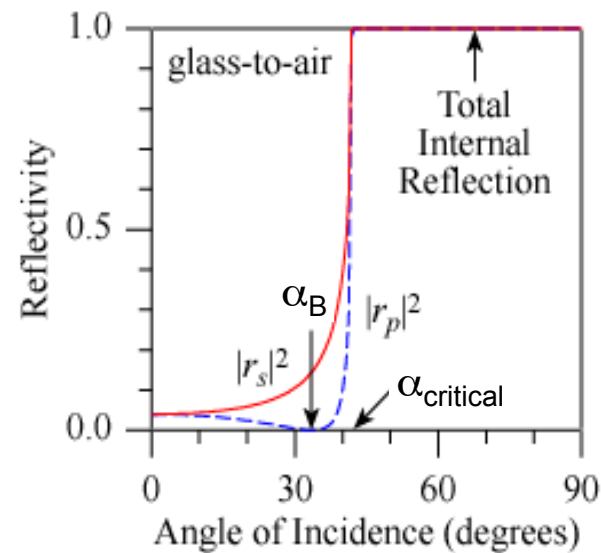
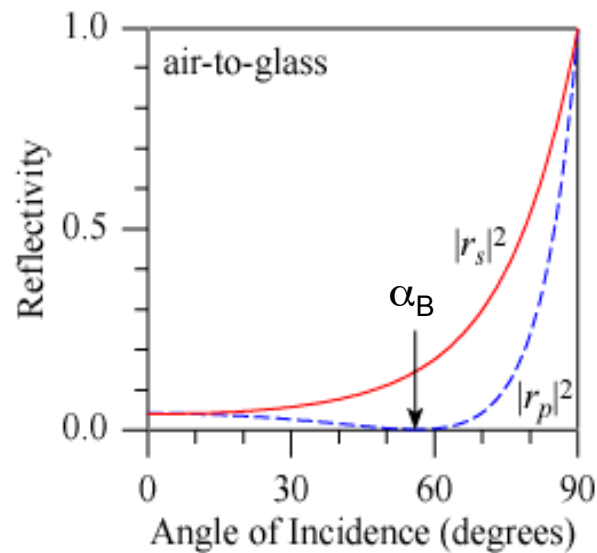


$$r_s = \left| \frac{E_{sr}}{E_{s1}} \right| = \frac{n_1 \cos \alpha_1 - n_2 \cos \alpha_2}{n_1 \cos \alpha_1 + n_2 \cos \alpha_2} \quad \Rightarrow \quad R_s = |r_s|^2$$

$$r_p = \left| \frac{E_{pr}}{E_{p1}} \right| = \frac{n_2 \cos \alpha_1 - n_1 \cos \alpha_2}{n_2 \cos \alpha_1 + n_1 \cos \alpha_2} \quad \Rightarrow \quad R_p = |r_p|^2$$

:: Polarization

e.g. reflection of polarized light at air/glass and glass/air

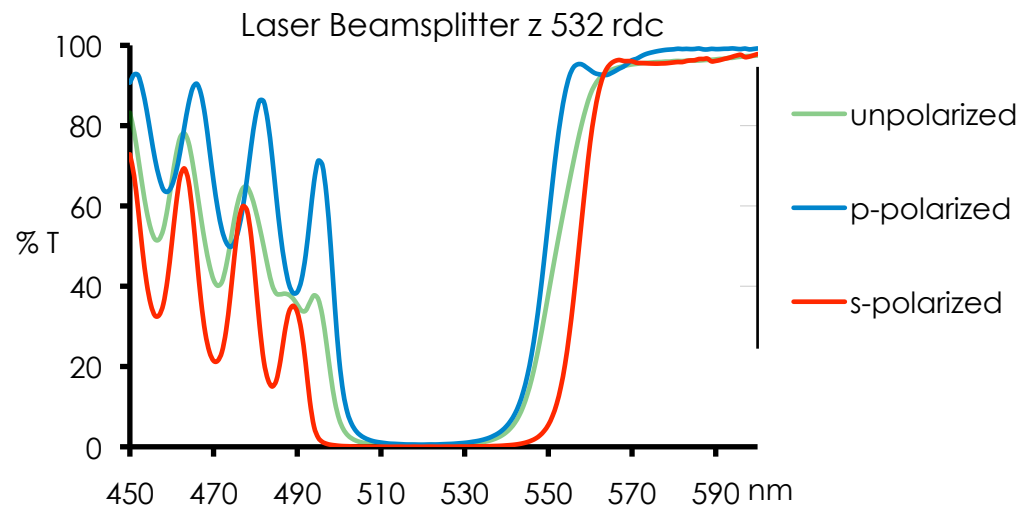


:: at the Brewster angle α_B p-polarized light is completely transmitted

:: Polarization

Influence on optical filters and beamsplitters

- :: s-polarized light can be better reflected than p-polarized light, if AOI $\neq 0$ degrees
- :: p-polarized light can be better transmitted (transmitted laser p-pol., reflected laser s-pol.)
- :: 45 degrees optical components are not applicable, if high blocking is required
- :: optical components working under AOI close to 0 degrees have steeper edges, because the s- and p-splitting is very small



:: Polarization

Influence on optical filters and beamsplitters

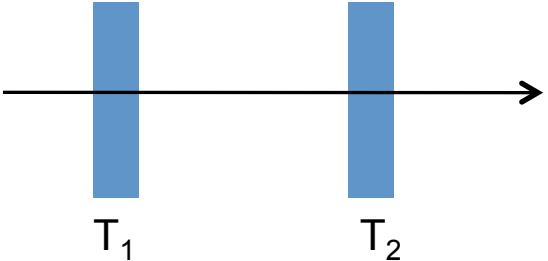
:: amplitude $r_s \neq r_p \Rightarrow$ the amount of s- and p-polarized light is changed, but there is no change of the polarization state

:: phase $\Phi_s \neq \Phi_p \Rightarrow$ the polarization state is changed (birefringent, e.g. $\lambda/4$ -plates)

:: Combining filters

Does it make sense?

:: combining filters with no loss of light



$$\frac{1}{T} = \frac{1}{T_1} + \frac{1}{T_2} - 1$$

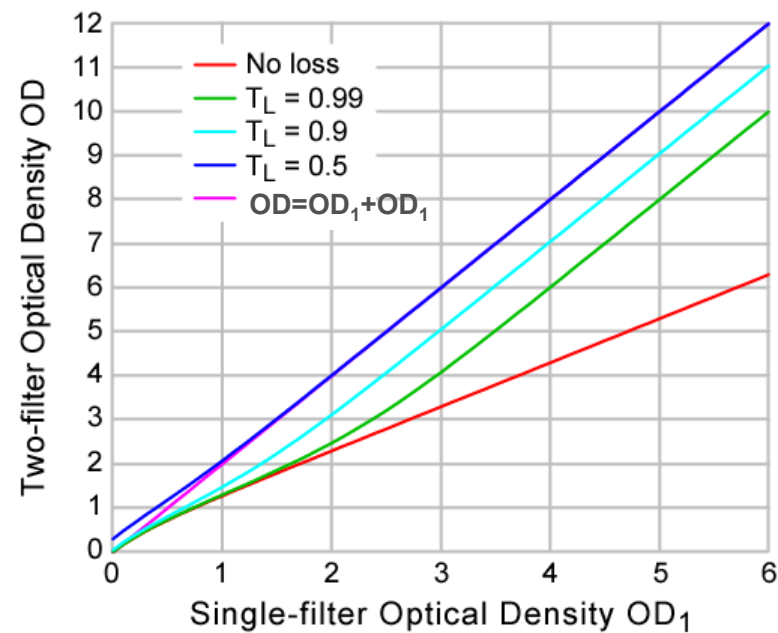
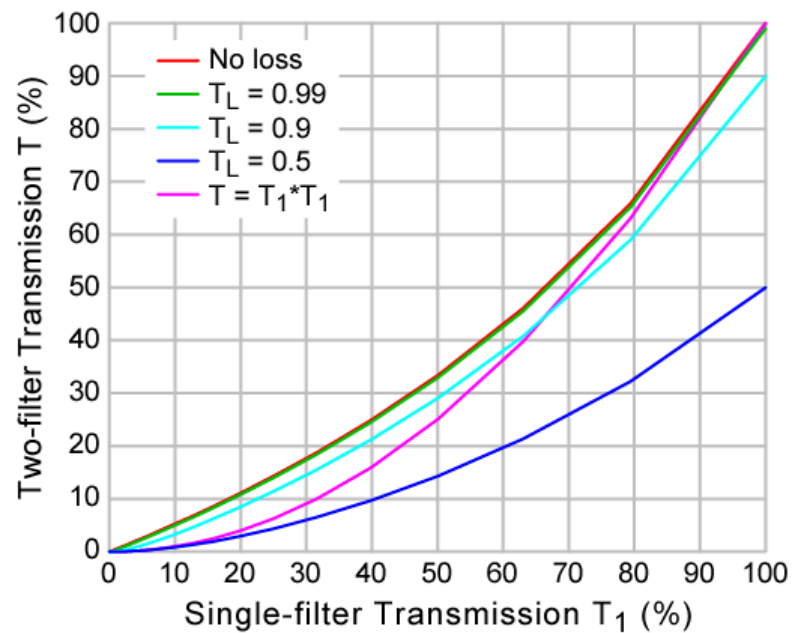
only for $T > 80\%$: $T = T_1 \cdot T_2$

$$OD = \log_{10}(10^{OD_1} + 10^{OD_2} - 1) \quad \text{not } OD = OD_1 + OD_2$$

:: e.g. both filters have 80% transmission and block with OD 4: $T = 66,6\%$ and $OD = 4,3$

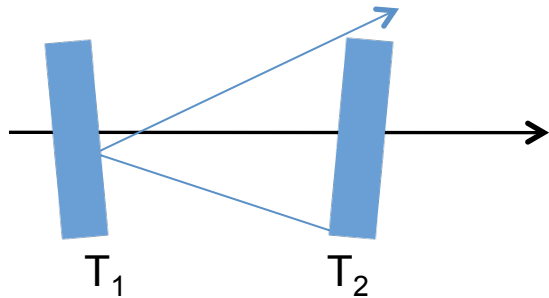
:: Combining filters

:: adding loss (tilting filters or adding absorption glass) increases blocking, but reduces transmission



:: Combining filters

possible setup for stacked filters



:: 100% loss of reflected light

:: in this case $OD = OD_1 + OD_2$

:: Our experience – your profit

:: Thank you very much

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